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Mathematics & Statistics 1 - March 2010

Time : 2 Hrs.

Max. Marks : 40

Q. 1 (A) Attempt any TWO of the following : [8]

(i) Which of the following sentences are statements ? (3)

(a) A cyclic trapezium has its non-parallel sides congruent.

(b) Do you like Mathematics ?

(c) The sun rises in the east.

(ii) Determine whether the following statement pattern is a 'tautology' or a 'contradiction' or 'neither' of the two : $(\neg p \vee q) \rightarrow p \wedge (q \vee \neg q)$ (3)

(iii) Using the truth table, show that $\neg(p \leftrightarrow q) = (p \wedge \neg q) \vee (q \wedge \neg p)$ (3)

(B) Attempt any ONE of the following : (2)

(i) Find the values of k if the lines represented by $K(x^2 + y^2) = 8xy$ are co-incident.

(ii) Find the lengths of intercepts made by the circle $x^2 + y^2 + 2x - 2y - 3 = 0$ on the co-ordinate axes. (2)

Q. 2 (A) Attempt any TWO of the following : [8]

(i) Find 'P' if the vectors $\vec{i} + \vec{j} - 3\vec{k}$, $2\vec{i} + \vec{j} - 4\vec{k}$ and $\vec{i} - \vec{j} + \vec{k}$ are co-planar. (3)

(ii) Using Vector method, show that the "medians of a triangle are concurrent." (3)

(iii) If $\vec{a}$, $\vec{b}$, $\vec{c}$ are three non-zero, non-coplanar vectors, then prove that and vector $\vec{r}$ in the space can be uniquely expressed as a linear combination $x\vec{a} + y\vec{b} + z\vec{c}$, where x , y and z are scalars. (3)

(B) Attempt any ONE of the following : (2)

(i) If D is the mid-point of seg AB and E is the mid-point of seg CD, then show that $\vec{AC} + \vec{BD} = 2\vec{DE}$.

(ii) Find the volume of the parallelepiped formed by the vectors $\vec{a} = \vec{i} + 2\vec{j} + 3\vec{k}$, $\vec{b} = 2\vec{i} + \vec{j} + 4\vec{k}$ and $\vec{c} = 3\vec{i} + 4\vec{j} + \vec{k}$. (2)

Q. 3 (A) (a) Attempt any ONE of the following : [8]

(i) If $A = \begin{bmatrix} 4 & 3 & 3 \\ -1 & 0 & -1 \\ -4 & -4 & -3 \end{bmatrix}$, then find A^{-1} by Adjoint method. (3)

(ii) Solve the following equations by Reduction method. $x - y + z = 2$, $2x + y - z = 7$, $x + 2y + z = 8$ (3)

(b) Attempt any ONE of the following : (2)

(i) If θ is the measure of acute angle between the lines represented by $ax^2 + 2kxy + by^2 = 0$, then show that $\tan \theta = \frac{2\sqrt{b^2 - ab}}{a + b}$ (3)

(ii) Find equation of a tangent to the circle $x^2 + y^2 + 2gx + 2fy + c = 0$ at the point $P(x_1, y_1)$. (3)

(B) Attempt any ONE of the following : (2)

(i) A dealer wishes to purchase a number of fans and sewing machines. He has only Rs. 5,760 to invest and has space for 20 items only. A fan costs Rs. 360 and a sewing machine costs Rs. 240. His expectation is that he can sell a fan at a profit of Rs. 22 and a sewing machine at a profit of Rs. 18. Assuming that he can sell all items that he can buy, formulate this problem as a L.P.P. to maximize his profit. (2)

(ii) Two food products A and B are to be purchased. Their contents and price per unit are given in the following table. (2)

Product	A	B
Calories	2	3
Vitamins	2	1
Price	3	4

Minimum requirements of calories and vitamins are 36 and 14 units respectively. Formulate this problem as a L.P.P. to minimize the cost.

Q. 4 (A) (a) Attempt any ONE of the following : [8]

(i) Find the values of p and q if the equation $12x^2 + 7xy - py^2 + 18x + qy + 6 = 0$ represents a pair of perpendicular lines. (3)

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30 (Continued) Mathematics & Statistics Paper I

Model	1	2	3	4	5	6	7	8	9	10
M1	1	2	3	4	5	6	7	8	9	10
M2	1	2	3	4	5	6	7	8	9	10
M3	1	2	3	4	5	6	7	8	9	10

Q.3 (A) Attempt any ONE of the following : [8]

(i) A company manufactures two models of fans, Model A and Model B. To stay in business, it must produce at least 100 fans of each model per month. The demand for fans is at least 150 fans of model A and 100 fans of model B per month. The total demand for both models is at least 250 fans per month.

The profit per fan is Rs. 400 for model A and Rs. 300 for model B. It is required to determine the number of fans of each type to be manufactured so as to get maximum profit. Formulate this problem as a L.P.P.

(ii) Represent graphically the feasible region of the inequalities $x + y \leq 4$, $x + 2y \leq 4$, $x \geq 0$, $y \geq 0$. Also find the coordinates of the vertices of the feasible region.

(B) Attempt any ONE of the following : (2)

(i) If for a binomial distribution probability of success is $\frac{1}{2}$ and the mean is 12.5, find the remaining parameters of the distribution. (2)

(ii) The probability that a man is a member of a club is $\frac{1}{3}$. Find the probability that a man is a member of a club and a woman is a member of a club. (2)

(iii) For the given data with the means $\bar{x}$ and $\bar{y}$, find the value of $\bar{z}$ if the data is as follows, where $\bar{z}$ is the mean of the data. (4)

x	y	z
10	20	30
20	30	40
30	40	50
40	50	60
50	60	70
60	70	80
70	80	90
80	90	100

Q.4 (A) Attempt any ONE of the following : [8]

(i) If X is a Poisson random variable such that $P(X=1) = P(X=2)$, find the mean and standard deviation of the distribution. (2)

(ii) If X is a Poisson random variable with mean 1, find $P(X \geq 2)$. [Given: $e^{-1} = 0.3679$] (2)

(B) Attempt any ONE of the following : (2)

(i) A company has two types of products, A and B, with the following data. (2)

Group	Year	Price	Quantity	Current year
Food and Clothing	2000	40	3	70
	2001	30	2	60
Household	2000	20	2	40
	2001	20	2	40

(ii) A person started Rs. 10,000 per month in the year 2001. What should be his saving per month in the year 2002 so as to maintain his income (i.e. of the year 2001) constant?

(C) Attempt any ONE of the following : (2)

(i) Find the value of $\bar{x}$ if the following data is as follows. (2)

x	f
10	1
20	2
30	3
40	4
50	5
60	6
70	7
80	8
90	9
100	10

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Q. 6.(B) Attempt any TWO of the following: [8]

(i) Ranking of 8 trainees at the beginning (X) and at the end (Y) of a certain course are given below : (4)

Trainees	A	B	C	D	E	F	G	H
X	1	2	4	5	6	8	3	7
Y	2	4	3	7	8	1	5	6

Calculate Spearman's rank correlation coefficient. (4)

(ii) A computer centre has four expert programmers. The centre needs four application programmes to be developed. The head of the computer centre, after studying carefully the programmes to be developed, estimates the computer time in minutes required by the experts to develop the application programmes as follows : (4)

Programmers	Programmes			
	1	2	3	4
	Times in minutes			
A	120	100	80	90
B	80	90	110	70
C	110	140	120	100
D	90	90	80	90

How should the head of the computer centre assign the programmes to the programmers so that the total time required is minimum ? (4)

(iii) From the data of 7 pairs of observations on X and Y following results are obtained : (4)

$$\sum (x_i - 70) = -38; \quad \sum (y_i - 60) = -5; \quad \sum (x_i - 70)^2 = 2990;$$
$$\sum (y_i - 60)^2 = 475; \quad \sum (x_i - 70)(y_i - 60) = 1063.$$

Obtain : (4)

(a) The line of regression of Y on X.

(b) The line of regression of X on Y.

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(3) Staffing is mainly related with.....

(4) To provide quality goods in the social responsibility of business organisation towards

(5) World Trade Organisation was established in the year

(B) Write a word or a phrase or a term which can be suitable for each one of the following statements : (5)

(1) State the name of commission which settles the claims of the consumers of more than 1 crore.

(2) State the level of management in which chief executives are involved.

(3) State the name of the expert who put forth 14 principles of management.

(4) The person who developed the concept of Total Quality Management.

(5) The Head of the Joint Hindu Family Business.

Q. 2. Write short notes on any THREE of the following : [15]

(1) Features of Disorganised Management.

(2) Importance of Communication.

(3) Problems in Consumer.

(4) Evolving Management.

(5) Need of Liberalisation.

Q. 3. Distinguish between the following. (Any THREE) : [15]

(1) Joint Hindu Family Business and Sole Trading Concern.

(2) Controlling and Directing.

(3) State Commission and National Commission.

(4) Lower Level Management and Middle Level Management.

(5) Statutory Corporation and Government Department.

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